

# Recipe for Success: 1-D Algebraic Kinematics

## One-Dimensional Problem-Solving Procedures

1. Read the problem carefully to determine whether the motion is **Uniform Motion** or **Uniform Accelerated Motion**. The first step of your solution is to write down “UM” or “UAM.”

2. If solving a Uniform Motion problem, write out

$x =$   
 $v =$   
 $t =$

If solving a Uniform Accelerated Motion problem, write out

$x =$   
 $v_0 =$   
 $v =$   
 $a =$   
 $t =$

3. Read the problem again and fill in as many values as you can (e.g.,  $x = 25$  m,  $v_0 = 5$  m/s,  $t = 7$  s, etc.).

4. From the problem, determine which quantity you are asked to calculate and draw a box around it.

5. If UM, write out the UM equation:  $v = x/t$ . If UAM, select the correct equation for your problem from the five UAM equations by the “who cares” quantity method: choose the equation that doesn’t include the “who cares” quantity (the quantity you don’t know and *aren’t* looking for). See “PhyzGuide: Algebraic Kinematics” for equations and further details.

6. After writing the correct equation for your problem, **WAIT!** Don’t put the numbers in just yet! Arrange the equation to solve for the quantity you’re seeking (i.e., if you have a UM problem in which you are given  $v$  and  $t$  and asked to find  $x$ , you must rearrange the UM equation  $v = x/t$  to  $x = vt$  before substituting the values of  $v$  and  $t$ ). **SOLVE FOR THE LETTERS FIRST!!!**

7. **SOLVE FOR THE LETTERS FIRST! REALLY, I MEAN IT!!!**

8. **DON’T PUT THE NUMBERS IN UNTIL YOU HAVE AN EQUATION THAT SOLVES FOR THE UNKNOWN QUANTITY IN TERMS OF THE KNOWN QUANTITIES! I’M NOT KIDDING!!!**

9. *After* you have an equation for the unknown quantity in terms of the known quantities, rewrite the equation substituting the values for the variables (i.e., if  $v = 15$  m/s and  $t = 3$  s,  $x = vt$  is rewritten as  $x = 15$  m/s  $\cdot$  3 s).

10. Calculate, write down the final answer, and box it!

# Recipe for Success: 2-D Algebraic Kinematics

## Two-Dimensional Problem-Solving Procedures

1. In a two-dimensional problem, you are given some sort of projectile that moves with constant speed in the horizontal ( $x$ ) direction while accelerating due to gravity in the vertical ( $y$ ) direction. Therefore, you have two simultaneous problems: an  $x$  problem (UM), and a  $y$  problem (UAM).

2. So write out

|         |            |
|---------|------------|
| x: UM   | y: UAM     |
| $x =$   | $y =$      |
| $v_x =$ | $v_{0y} =$ |
|         | $v_y =$    |
|         | $a =$      |
| $t =$   |            |

3. List all the quantities as you would in a 1-D problem. There is a probability (which borders on certainty) that the time of the projectile's flight will not be given. Time is the link between the  $x$  and  $y$  motions: the projectile's flight lasts for a certain amount of time. Time is not an  $x$ -quantity nor is it a  $y$ -quantity; time is a unifying quantity. So the trick of these problems is usually to determine the time using one motion (the  $x$  or  $y$ ) then substitute that information to solve for an unknown quantity involving the other motion ( $y$  or  $x$ ).

The key to solving the problem is often finding the time of flight for the projectile. To do this, you must ask yourself this: When the flight ended, was it prevented from advancing in the  $x$ -direction or in the  $y$ -direction? For example, when a dart is thrown, its motion is eventually hindered in the  $x$ -direction—the dartboard stops the dart from advancing further. If a ball rolls off a table and becomes a projectile, its  $y$ -motion is eventually prevented from advancing by the floor. If the  $x$ -motion is hindered, use the  $x$  motion (UM) to determine the time; if the  $y$ -motion is hindered, use the  $y$ -motion (UAM) to determine the time.

4. Once you've developed an expression for time  $t$  using one motion (ex:  $y$ -motion), use that expression for  $t$  when solving the other motion (ex:  $x$ -motion).

5. Treat that "other" motion as if it were a one-dimensional kinematics problem. See "Recipe for Success: 1-D Algebraic Kinematics" for details.

6. Calculate, write down the final answer, and box it!